

## Day 54 Bellwork: Have your homework out and then complete the following

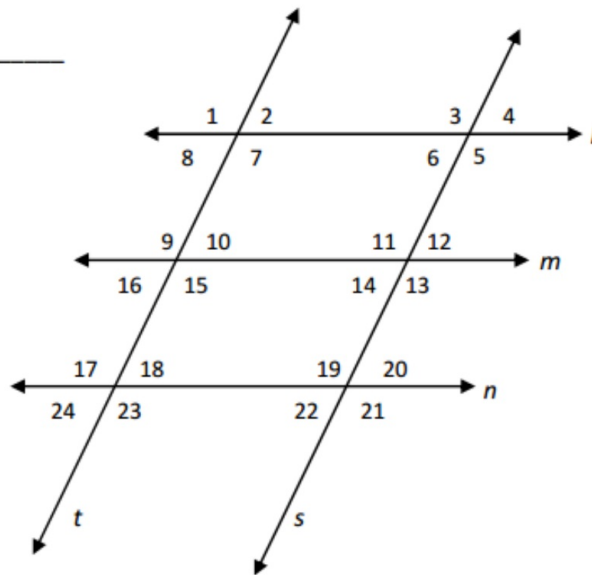


1. Given  $l \parallel m \parallel n$  and  $s \parallel t$ , and  $m\angle 1 = 143^\circ$ , find

$$m\angle 2 = \underline{\hspace{2cm}} \quad m\angle 11 = \underline{\hspace{2cm}} \quad m\angle 20 = \underline{\hspace{2cm}}$$

$$m\angle 3 = \underline{\hspace{2cm}} \quad m\angle 12 = \underline{\hspace{2cm}} \quad m\angle 21 = \underline{\hspace{2cm}}$$

2. Is  $x - 5$  a factor of the function  
 $f(x) = x^3 + x^2 - 27x - 15$ ?  
 Show work supporting your answer.



Before we dive in, here are two important properties:

Substitution:  $a + b = \text{blah}$     $c + d = \text{blah}$

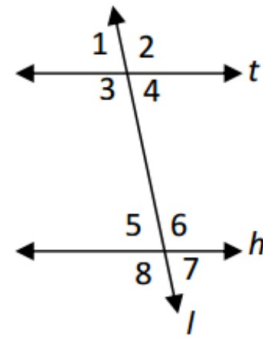
$$a + b = c + d$$

Transitive:  $a = b$    and    $b = c$    then    $a = c$

1. Given:  $t \parallel h$

Prove:  $\angle 3 \cong \angle 6$

| Statement                    | Reason                         |
|------------------------------|--------------------------------|
| 1. $t \parallel h$           | Given                          |
| 2. $\angle 3 \cong \angle 8$ | Corresponding $\angle$ s post. |
| 3. $\angle 8 \cong \angle 6$ |                                |
| 4. $\angle 3 \cong \angle 6$ |                                |



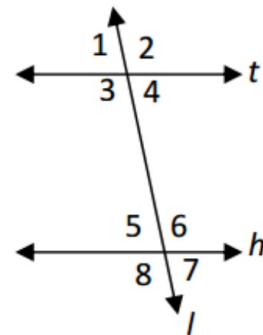
2. Given:  $t \parallel h$

Prove:  $\angle 2 \cong \angle 8$

3. Given:  $t \parallel h$

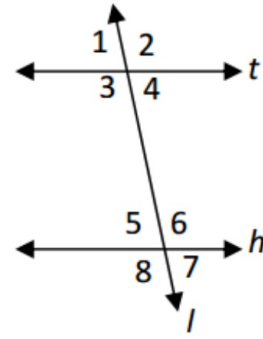
Prove:  $\angle 3$  and  $\angle 5$  are supplementary

| Statement                              | Reason |
|--|--------|
| 1. $t \parallel h$                     |        |
| 2. $\angle 3 \cong \angle 8$           |        |
| 3. $m\angle 3 = m\angle 8$             |        |
| 4. $\angle 8$ and $\angle 5$ are supp. |        |
| 5. $m\angle 8 + m\angle 5 = 180^\circ$ |        |
| 6. $m\angle 3 + m\angle 5 = 180^\circ$ |        |
| 7. $\angle 3$ and $\angle 5$ are supp. |        |



4. Given:  $t \parallel h$

Prove:  $\angle 2$  and  $\angle 7$  are supplementary



We have 5 theorems to prove 's  
4 of them are...

SSS

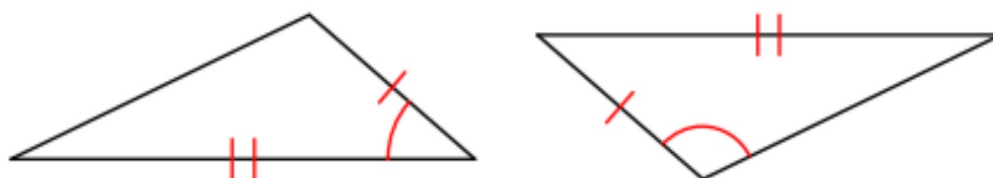
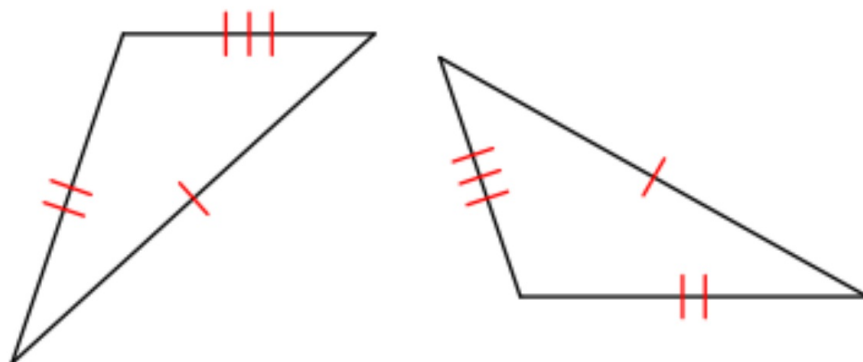
ASA

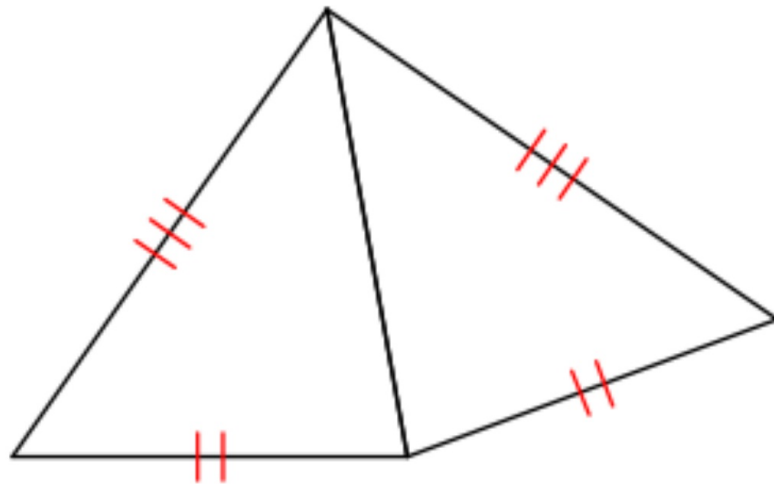
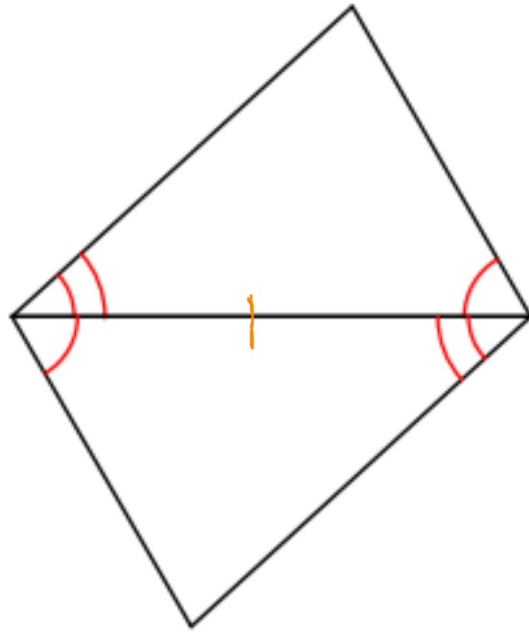
SAS

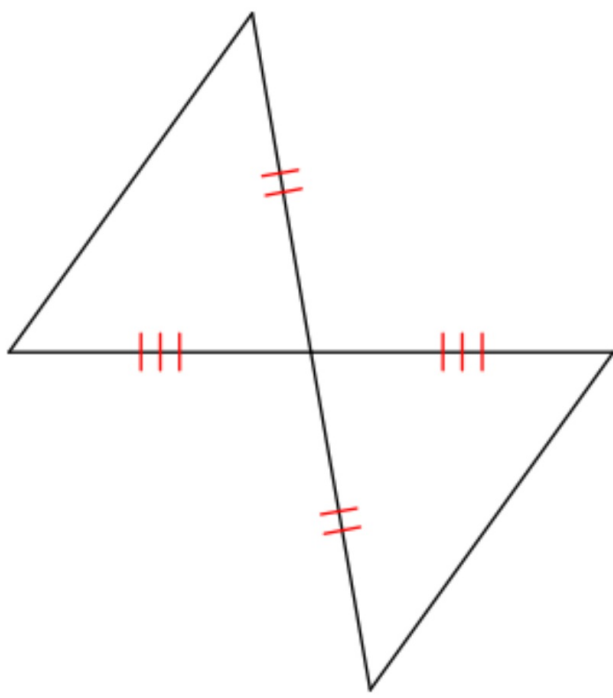
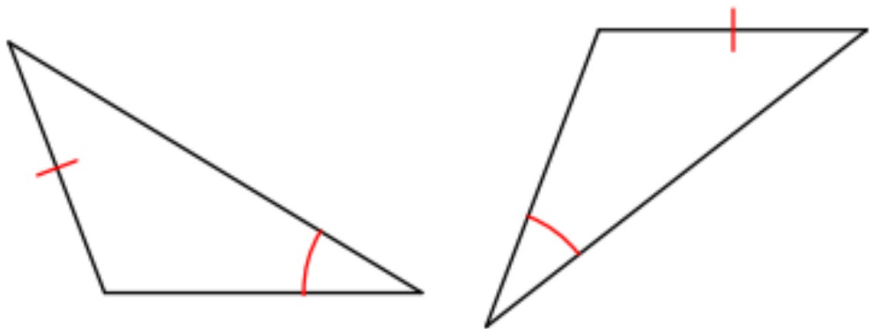
AAS

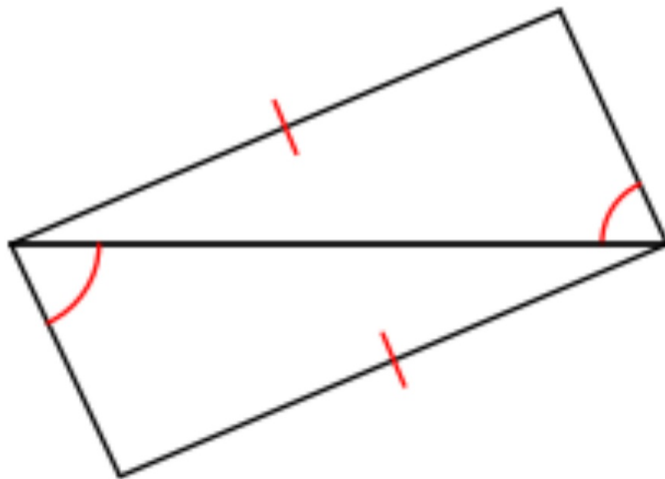
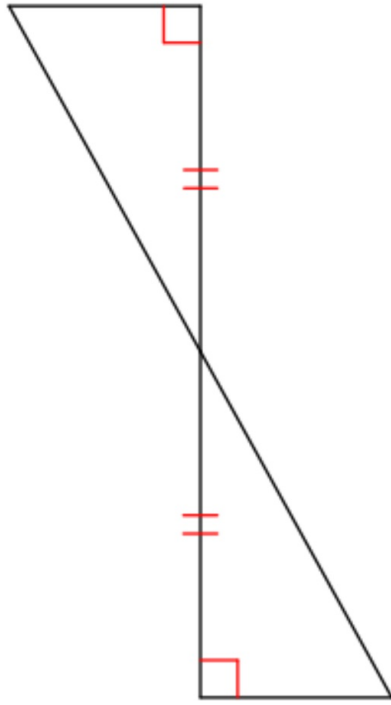


**Guess how the triangles are congruent...**









**Fin.**



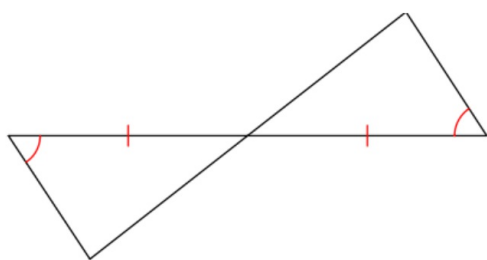
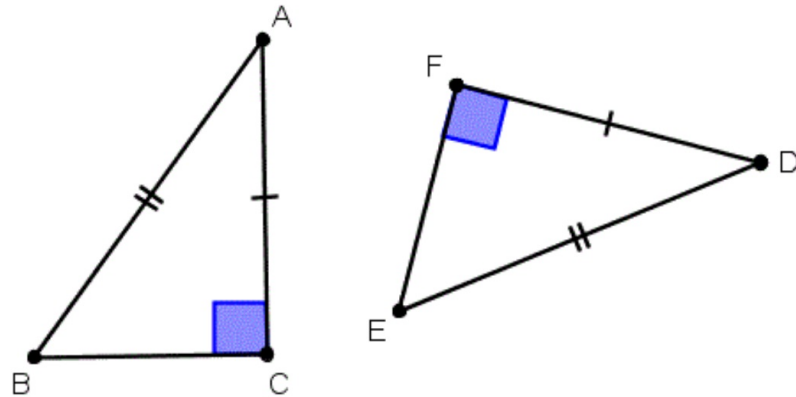
**But Angle Side Side DOES  
EXIST when the angle is  
just RIGHT!**





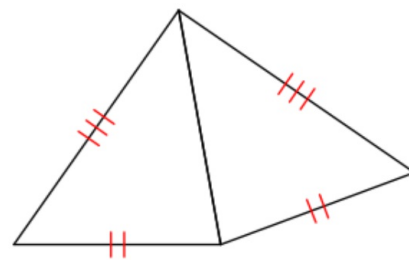
## Hypotenuse Leg is the 5th postulate

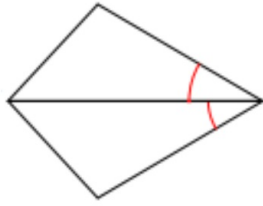
Picture:



## Vertical Angle Property

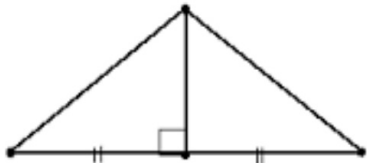
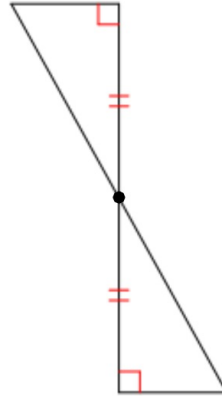
Reflexive Property





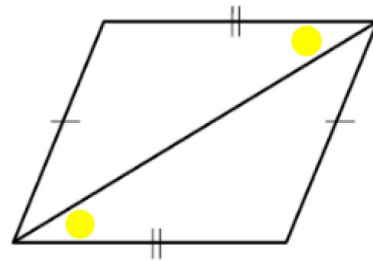
**Definition of  
Bisector**

**Definition of  
Midpoint**



**Definition of  
Perpendicular Bisector**

**Alternate Interior  
Angles**

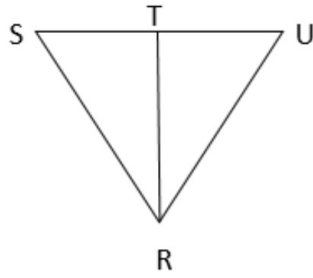


1) Given:

$RS \cong RU, TS \cong TU, \angle S \cong \angle U, \angle SRT \cong \angle URT$

Prove:

$\Delta RST \cong \Delta RUT$

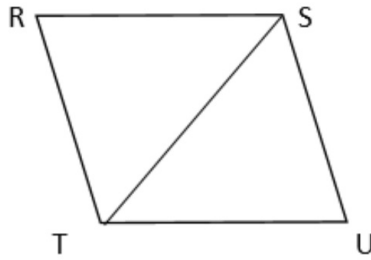


2) Given:

$RS \cong UT, RT \cong SU$

Prove:

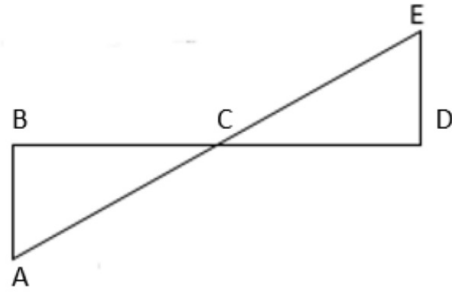
$\Delta RST \cong \Delta UTS$



3) Given:  $\angle B$  &  $\angle D$  are  $90^\circ$ ,  $AE$  bisects  $BD$

Prove:

$\triangle ABC \cong \triangle EDC$

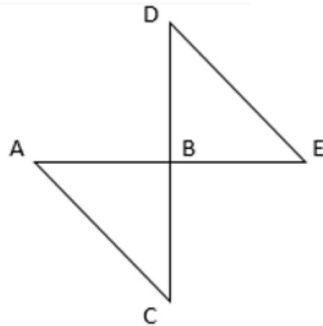


4) Given:

$DC \perp AE$ ,  $DE \cong AC$ ,  $B$  is the midpoint of  $AE$

Prove:

$\triangle BDE \cong \triangle BCA$

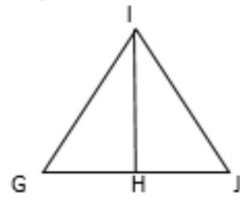


5) Given:

$H$  is the midpoint of  $GJ$ ,  $GI \cong IJ$

Prove:

$\triangle GHI \cong \triangle JHI$

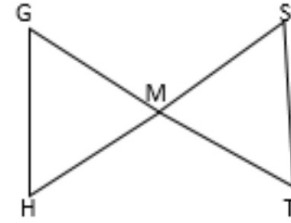


6) Given:

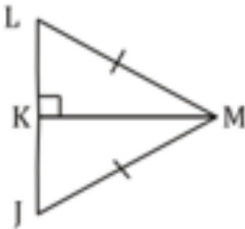
$M$  is the midpoint of  $GT$ ,  $M$  is the midpoint of  $HS$

Prove:

$\triangle GMH \cong \triangle TMS$

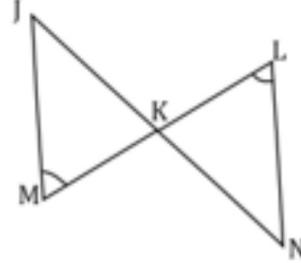


7) Given:  $\overline{LM} \cong \overline{JM}$



Prove:  $\triangle LKM \cong \triangle JKM$

8) Given:  $\overline{JN}$  Bisects  $\overline{ML}$ ,  $\angle M \cong \angle L$



Prove:  $\triangle MJK \cong \triangle LNK$